

Quantum theory of coherent transverse optical magnetism: erratum

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Several corrections of detail are made to an earlier paper. The main results and conclusions are unchanged.

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For irreducible field components to be represented consistently throughout Ref. [1], the conjugation of some Rabi frequencies must be corrected in Eqs. (20), (21), (24), and (25).

$$V_{12}^{(e)} \equiv \langle 1|V^{(e)}|2\rangle = -\frac{1}{2}\hbar\langle 1|[\Omega_+^{(e)} + \Omega_-^{(e)}]e^{i\varphi} + h.c.|2\rangle, \quad (20)$$

$$V_{12}^{(m)} \equiv \langle 1|V^{(m)}|2\rangle = -\frac{1}{2}\hbar\langle 1|[\Omega_+^{*(m)} + \Omega_-^{*(m)}] + h.c.|2\rangle \\ -\frac{1}{2}\hbar\langle 1|[\Omega_+^{(m)} + \Omega_-^{(m)}]e^{2i\varphi} + h.c.|2\rangle, \quad (21)$$

$$\rho_{12}^{(e)} = \frac{1}{2} \left\{ \frac{[\Omega_+^{(e)} + \Omega_-^{(e)}]_{12}}{(\Delta_1 + i\Gamma_{12})} e^{i\omega t} \right\} (\rho_{11} - \rho_{22}), \quad (24)$$

$$\rho_{12}^{(m)} = \frac{1}{2} \left\{ \frac{[\Omega_+^{(m)} + \Omega_-^{(m)}]_{12}}{(\omega_\varphi + i\Gamma_{12}^{(m)})} e^{-i\omega t} \right. \\ \left. + \frac{[\Omega_+^{(m)} + \Omega_-^{(m)}]_{12}}{(\Delta_2 + i\Gamma_{12}^{(m)})} e^{i\omega t} \right\} (\rho_{11}^{(0)} - \rho_{22}^{(0)}). \quad (25)$$

The asterisk in Eq. (26) should be dropped. The same notational correction is needed in the sentence, “Hence the specific replacement $\Omega_0^{(m)} = [\Omega_+^{(m)} + \Omega_-^{(m)}]$ has been made for the magnetic term, and $\Omega_0^{(e)} = \frac{1}{2}[\Omega_+^{(e)} + \Omega_-^{(e)}]$ for the electric term.”

The subscript on resonant frequency ω_0 in Eqs. (25), (28), (30), and (42) should be φ , not 0, to denote the *ground state* resonant frequency ω_φ of magnetically induced torsional vibrations that are azimuthal with respect to the optical B field:

$$\bar{M}(t) = -\hat{y} \left(\frac{Ne}{2m} \right) \left\{ \frac{1}{2} \left[\frac{\langle 2|L_y|1\rangle[\Omega_0^{(e)}]_{12}[\Omega_0^{(m)}]_{12}}{(\Delta_1 + i\Gamma_{12}^{(e)})(\Delta_2 + i\Gamma_{12}^{(m)})} e^{i\omega t} \right. \right. \\ \left. \left. + \frac{\langle 2|L_y|1\rangle[\Omega_0^{(e)}]_{12}[\Omega_0^{(m)*}]_{12}}{(\omega_\varphi + i\Gamma_{12}^{(m)})(\Delta_2 + i\Gamma_{12}^{(m)})} e^{-i\omega t} \right] + h.c. \right\} (\rho_{11} - \rho_{22}), \quad (28)$$

$$\tilde{M} = -\hat{y} \left(\frac{Ne}{m} \right) \frac{1}{2} \left[\frac{\langle 2|L_y|1\rangle[\Omega_0^{(e)}]_{12}[\Omega_0^{(m)}]_{12}}{(\Delta_1 + i\Gamma_{12}^{(e)})(\Delta_2 + i\Gamma_{12}^{(m)})} \right. \\ \left. + \frac{\langle 2|L_y|1\rangle^*[\Omega_0^{*(e)}]_{12}[\Omega_0^{(m)*}]_{12}}{(\omega_\varphi - i\Gamma_{12}^{(m)})(\Delta_2 - i\Gamma_{12}^{(m)})} \right] (\rho_{11} - \rho_{22}). \quad (30)$$

Similarly, ω_0 should be ω_φ in the sentence, “We also note that the second term in Eq. (30) is much smaller than the first due to the ω_φ factor in the denominator (unless ω_φ is small compared to Δ_1).”

The exponential time factors were interchanged in Eq. (42). It should read

$$\bar{P}(t) = N\hat{z}(\mu_{21}^{(e)}\rho_{12}^{(m)}(t)\rho_{12}^{(e)} + h.c.) \\ = N\hat{z} \left\{ \left(\frac{1}{2} \frac{\mu_{21}^{(e)}[\Omega_0^{(m)}]_{12}[\Omega_0^{(e)}]_{12}}{(\Delta_1 + i\Gamma_{12}^{(e)})(\omega_\varphi + i\Gamma_{12}^{(m)})} + h.c. \right) \right. \\ \left. + \left(\frac{1}{2} \frac{\mu_{21}^{(e)}[\Omega_0^{(m)}]_{12}[\Omega_0^{(e)}]_{12}}{(\Delta_1 + i\Gamma_{12}^{(e)})(\Delta_2 + i\Gamma_{12}^{(m)})} e^{2i\omega t} + h.c. \right) \right\}. \quad (42)$$

The conclusions from Eq. (42) regarding frequency-dependent enhancement of magnetic effects were similarly interchanged. The discussion should state, “Just like

the magnetization at frequency ω in Eq. (31), the second harmonic signal is longitudinally polarized and contains the parametric resonance factor $[\Delta_2 + i\Gamma_{12}^{(m)}]^{-1}$. The first term is a zero frequency interaction that predicts a static charge separation induced in dielectric media by moderately intense light. Since it is inversely proportional to ω_φ , its magnitude may be strongly enhanced when this quan-

tity is small." All other results and conclusions of the paper are unchanged.

REFERENCES

1. S. C. Rand, "Quantum theory of coherent transverse optical magnetism," *J. Opt. Soc. Am. B* **26**, B120–B129 (2009).